ChemStor: Using Formal Methods to Guarantee Safe Storage and Disposal of Chemicals

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Abstract

While safe chemical storage and disposal are simple in principle—users should read safety specifications and place chemicals in appropriate cabinets or collection points—high-profile incidents involving improper storage and disposal of chemicals continue to occur. This paper introduces *ChemStor*, an open-source, automated computational system that can guarantee (mathematically verify a system is correct with respect to its specification), with regard to prescribed constraints, safe storage and disposal of chemicals used in academic, industrial, and domestic settings. *ChemStor* borrows concepts from formal methods—a branch of computer science capable of mathematically proving a specification or software is correct—to safely store or dispose of chemicals. If two or more chemicals can be combined in the same cabinet without forming possibly dangerous combinations of chemicals (while observing cabinet/shelf space constraints), then *ChemStor* determines that the storage configuration is safe. Likewise, if chemicals can be added to an existing disposal container without forming possibly dangerous combinations of chemicals (or exceeding the volume of the container), then *ChemStor* determines that the disposal configuration is safe. *ChemStor* accomplishes this by first building a chemical interaction graph, a graph that describes which chemicals may interact with each other based on their Reactivity Groups as determined by the United States Environmental Protection Agency. Next, *ChemStor* computes the chromatic number of the graph, the smallest number of colors used to color the graph such that no two vertices (chemicals) that share an edge (an interaction) share the same color. *ChemStor* then assigns all the chemicals of each color to a storage or disposal container after confirming that there is enough space in the container. These steps are encoded into a series of Satisfiability Modulo Theory equations, and *ChemStor* uses an industry-standard tool to try to find a valid solution to these equations. The result is either a solution which dictates exactly where to store or dispose of each chemical, or an indication that no safe storage or disposal configuration could be found. To demonstrate the feasibility of *ChemStor*, we used the tool to analyze ten real-world chemical...
storage and disposal incidents that led to injuries or destruction of property. In each case, ChemStor quickly and successfully identified a proper chemical disposal or storage configuration that would have prevented the incident. In the future, ChemStor may be integrated with electronic laboratory notebooks, voice assistants, and other emerging technology to protect users of chemicals in labs, workplaces, and homes.

1 Introduction

Many common chemicals can undergo dangerous reactions when combined with incompatible chemicals during storage or disposal. For example, millions of tons of nitric acid are produced every year, making it a ubiquitous chemical in many research and industrial settings. Likewise, millions of tons of organic solvents are produced every year and used in many different applications. But when nitric acid is mixed with organic solvents, hazardous chemical products, fires, and explosions can result. While all chemists are (hopefully!) trained to avoid intentionally mixing nitric acid and organic solvents, accidents sometimes occur when these chemicals are unintentionally mixed in a chemical storage location or a waste disposal container. Furthermore, nitric acid and organic solvents are just a few of the millions of chemicals that can undergo dangerous reactions when combined during storage or disposal. Incidents due to improper storage or disposal of chemicals occur with alarming frequency, with consequences like second-degree burns and destroyed laboratories.

Efforts to improve chemical safety generally fall into two categories—system-based approaches and behavioral approaches—both of which have limitations in avoiding storage- and disposal-related incidents:

- **System-based solutions** focus on building systems (often computer-based) that aid research labs in managing many different administrative functions involving chemicals. These functions may include generating various state and federal compliance reports, automatically issuing a purchase order should inventory of a chemical fall below preset
levels, and sharing inventory among collaborating laboratories. Some Chemical Inventory Management Systems (CIMS) employ simple safety features, like the ability to parse a chemical’s Materials Safety Data Sheet (MSDS) to inform the researcher how to properly store the chemical. Chempliance offers some guidelines on chemical disposal practices but is lacking any guarantees with respect to safety and does not track the volumes of chemicals.

- **Behavioral systems** focus on training and the human aspects of safety. Some of these systems train employees to focus on “safety first,” while others aim to identify disparities between institutional and individual beliefs about safety. These approaches focus on systemic issues that, while important, are sometimes relatively abstract and far removed from the specific day-to-day decisions faced by a researcher, like where to store a particular new chemical, or where to dispose of a certain waste chemical.

In summary, existing methods for improving chemical safety can inform researchers about general best practices, but fail to provide real-time guidance on specific storage and disposal decisions.

This paper introduces ChemStor, an open-source, automated chemical storage and disposal system that is provably safe with respect to proper laboratory safety protocols. For a given set of chemicals and containers, ChemStor either provides a specific storage or disposal configuration that is safe, or informs the user that no safe storage/disposal configuration is possible. Specifically, ChemStor informs users which specific cabinet or bin should be used to store or dispose of each chemical, thereby easing the burden of safety protocols that users must keep in their minds, while simultaneously minimizing the space required for chemical storage and disposal. ChemStor can be integrated with electronic laboratory notebooks, voice assistant tools, and many other existing and emerging technologies. Finally, ChemStor can enhance safety in a wide range of settings, not only research laboratories and industrial facilities, but also homes (where each year, mixing incompatible pool cleaning chemicals leads to an estimated 4,500 injuries alone).
2 Overview of ChemStor

In this section, we summarize the operation of ChemStor in the context of a specific safety incident. In 1997, while one of the authors (WHG) was a student at the University of Tennessee, Knoxville, students in an undergraduate chemistry laboratory performed the Belousov-Zhabotinsky (BZ) reaction:

\[ 3 \text{CH}_2(\text{CO}_2\text{H})_2 + 4 \text{BrO}_3^- \xrightarrow{\text{Ce}^{2+}} 4 \text{Br}^- + 9 \text{CO}_2 + 6 \text{H}_2\text{O} \quad (1) \]

The BZ reaction is commonly studied in laboratory classes due to its unusual oscillatory nature. As is typically done, the students at UT Knoxville combined aqueous solutions of malonic acid and potassium bromate along with a cerium ammonium nitrate catalyst. When the reactants are combined as aqueous solutions, the reaction is benign, and the laboratory class concluded without incident. However, during post-lab cleanup, spilled reactants in dry form were swept from around the laboratory balances and into a waste container. This container was subsequently placed beneath a leaky sink, which began adding drops of water to the mixture of dry reactants after the laboratory was empty. The resulting reaction was extremely exothermic and caused a fire that resulted in significant damage to the laboratory.

How could ChemStor have prevented this incident? More specifically, at the end of the laboratory class, after the dry reagents used in the BZ reaction were combined into the same waste container, how could ChemStor warn the teaching assistants that they should avoid any situation that might add water to this container (like placing the container beneath a leaky sink)?

The first step involves defining which chemicals are currently in which storage containers. Fig. 1A depicts the chemical storage situation at the end of the class, with the three dry reagents used in the BZ reaction (malonic acid, potassium bromate, and cerium ammonium nitrate) combined in a single chemical storage container, and the teaching assistant contemplating placing this container beneath a sink where water might be added to it.
Figure 1: Using *ChemStor* to safely dispose of leftover reactants from performing the Belousov-Zhabotinsky (BZ) reaction. This simple scenario (based on real-life events that culminated in a lab-destroying fire) begins with three reactants (cerium ammonium nitrate, malonic acid, and potassium bromate) combined in dry form in a single container (A). A teaching assistant considers placing this container beneath a leaky sink drain, which will add water to the mixture. At this point, *ChemStor* constructs a chemical interaction graph (B) containing vertices for each chemical in the proposed mixture. In this graph, chemicals that may react with each other are linked with solid lines, and chemicals that are identical and can be combined are linked with dotted lines. After *ChemStor* calculates the chromatic number of the graph and colors the graph (C), the chemicals can be safely added to different containers based on their vertex colors (D). At this point, *ChemStor* would notify the teaching assistant that water should *not* be added to the container with the BZ reactants, the teaching assistant would avoid placing the container in a wet location, and a significant laboratory accident would have been avoided.
Next, ChemStor builds a chemical interaction graph $G$ (Fig. 1B) containing 3 sets: a set of vertices, $V$; and two different sets of edges, $E$ and $A$:

- The vertices, $V$, are the individual chemicals in this scenario. Specifically, we can define the vertices $v = \text{cerium ammonium nitrate}$, $u = \text{malonic acid}$, $w = \text{potassium bromate}$, and $z = \text{water}$. We can furthermore say that $v \in V$, $u \in V$, $w \in V$, and $z \in V$, or that $v, u, w, z$ are members of, or are “in,” the set of vertices $V$. (The “$\in$” symbol, as well as the other standard Boolean logic and set theory symbols used in this work, are defined in Table 1.)

- The set $E$ is the set of edges that represent unsafe combinations of chemicals, or “interference” edges. Because mixing $v$, $u$, and $w$ without $z$ will not result in a dangerous reaction, it can be said that $(v, u) \notin E$; or that there is no edge between $v$ and $u$. Similarly, there is no edge between the other combinations of the dry BZ reactants, so $(u, w) \notin E$ and $(v, w) \notin E$. Interference edges are denoted as solid lines between vertices in Fig. 1B. In this example the teaching assistant is considering possibly adding water to a container that already contains the dry BZ reagents ($z$ and $z \in V$). Because $z$ (water) will lead to a dangerous reaction when added to the combined dry BZ reagents, there are edges between each of the BZ reactants and water, so $(v, z) \in E$, $(u, z) \in E$, and $(w, z) \in E$, as shown in Fig. 1B.

- The set $A$ is the set of edges that represent instances of the same chemical, properly defined as “affine” edges. The dotted line in Fig. 1B represents an affine edge. In this scenario, the edge represents some additional malonic acid ($a$) that requires disposal. Thus, $a \in V$, and $(u, a) \in A$ because both $u$ and $a$ are malonic acid and are chemically identical. The set of affine edges enables ChemStor to save chemical storage volume space by combining $u$ and $v$, assuming the container for $u$ or $v$ has enough space. ChemStor represents this as $\forall (u, v) \in A$ ($\forall$ reads “for all”).

Now that the chemical interaction graph $G$ has been built, ChemStor can calculate the
Table 1: Common notation in set theory and Boolean logic.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Plain English</th>
<th>Example</th>
<th>Outcome</th>
</tr>
</thead>
<tbody>
<tr>
<td>$</td>
<td>A</td>
<td>$</td>
<td>Cardinality</td>
</tr>
<tr>
<td>$\in$</td>
<td>Set membership</td>
<td>$1 \in \mathbb{N}$</td>
<td>Statement of fact — 1 is a member of the set of natural numbers</td>
</tr>
<tr>
<td>$\subseteq$</td>
<td>Subset or equal</td>
<td>$A \subseteq B$</td>
<td>Determines whether all the elements in set $A$ are also in set $B$</td>
</tr>
<tr>
<td>$A \setminus B$</td>
<td>Set difference</td>
<td>$A \setminus B$</td>
<td>Returns the elements in $B$ that are not in $A$</td>
</tr>
<tr>
<td>$\land$</td>
<td>Boolean AND</td>
<td>$X \land Y$</td>
<td>Evaluates true if and only if both predicates $X$ and $Y$ are true</td>
</tr>
<tr>
<td>$\lor$</td>
<td>Boolean OR</td>
<td>$X \lor Y$</td>
<td>Evaluates true if either and both predicates $X$, $Y$ are true</td>
</tr>
<tr>
<td>$\neg$</td>
<td>Boolean NOT</td>
<td>$\neg X$</td>
<td>Negates the predicate $X$. If $X$ is true, then $\neg X$ evaluates to false</td>
</tr>
<tr>
<td>$\forall$</td>
<td>For all</td>
<td>$\forall a(a &gt; 1)$</td>
<td>Definition of the natural numbers</td>
</tr>
<tr>
<td>$\exists$</td>
<td>There exists</td>
<td>$\forall (m \in \mathbb{N}) \exists (n \in \mathbb{N})(n &gt; m)$</td>
<td>The set of natural numbers continues ad infinitum</td>
</tr>
</tbody>
</table>

The smallest number of containers required for safe disposal of the chemicals in $G$. ChemStor accomplishes this by calculating the graph’s chromatic number, $\chi(G)$, a step in “coloring” the graph. Graph coloring is a mathematical problem that aims to color a graph’s vertices with the minimal number of different colors, while guaranteeing that no two vertices that share an edge also share the same color. For safe disposal or storage of chemicals, the only edges that are of consequence are the interference edges, or the solid edges in Fig. 1B. This graph is trivially small and can be colored by hand using two colors, as shown in Fig. 1C. However, graph coloring belongs to a class of problems that are incredibly difficult to solve efficiently, the so-called \textit{NP-complete} problems, so as more chemicals are added to the graph, the computational effort required to color the graph grows astronomically. The computational effort required to solve the graph coloring problem is proportional to $2^n$, where $n$ is the number of colors in the graph.
Finally, the graph’s chromatic number (the number of different colors on the colored graph) denotes the minimum number of containers required to safely dispose of the chemicals in the graph. In this example, ChemStor recommends placing water in a separate container, not in the container with the dry BZ reagents (Fig. 1D). If this information was then communicated to the teaching assistant, they might avoid placing the container in a location where water could be added, thereby avoiding a significant laboratory accident.

3 Methods

In this section, we present details on the necessary data structures, algorithms, and constraints used by ChemStor to determine the safe disposal and storage of chemicals.

3.1 Chemical Compatibility

To obtain information about which types of chemicals are compatible or incompatible with each other, ChemStor relies on a chemical classification system created jointly by the US Environmental Protection Agency (EPA) and National Oceanic and Atmospheric Administration (NOAA). This system categorizes over 9,800 chemicals into 68 reactivity groups that have similar properties. Mixing materials from certain reactivity groups can produce materials from other reactivity groups; for example mixing acids and bases induces a strong reaction that produces salt and water. The EPA/NOAA categorization assigns one of three outcomes to the combination of chemicals: Incompatible, Compatible, or Caution. We write \( \text{interact}(x, y) = \frac{1}{2} \) if chemicals \( x \) and \( y \) cause an adverse reaction (\( \frac{1}{2} \)) when mixed, or are Incompatible. Chemical combinations that result in Caution are either deferred to the expert user or treated as Incompatible. Finally, if either \( x \) or \( y \) (or both) are not classified with a reactivity group (in other words, they do not appear in the EPA/NOAA classification list), then the chemicals are marked as Unknown and ChemStor notifies the user that any possible storage or disposal solution would require review by an expert.
3.2 Chemical Interaction Graph

Let $G(V, E, A)$ be the chemical interference graph representing a storage problem. $V$ is the set of chemicals we desire to store, $E$ is the set of interference edges between incompatible chemicals, and $A$ is the set of affinity edges between unique instances of identical chemicals. An interference edge $(v, u)$ is added to $E$ if, for any two chemicals $v, u$, $\text{interact}(v, u) = \frac{1}{2}$ as noted in §3.1. An affinity edge $(v, w)$ is added to $A$ if $v$ and $w$ represent distinct instances of the exact same chemical (i.e., there is more than one container of a certain chemical we wish to store). The chemical interaction graph may be extended to include a set $P \subseteq V$ of vertices and $Q \subseteq E$ of edges representing chemicals already in storage and their corresponding edges, respectively.

3.3 Chemical Storage

Let $C = \{c_1, c_2, \ldots, c_k\}$ be the set of cabinets for chemical storage. Each cabinet contains a finite set of shelves. Let $S(c_m)$ denote the set of shelves within cabinet $c_m \in C$, where $s_{m}^{n}$ denotes the $n^{th}$ shelf in $c_m$. Each shelf $s_{m}^{n} \in S(c_m)$ has an immutable capacity, denoted $\text{maxCapacity}(s_{m}^{n})$ with which it can use to store chemicals. The capacity of each cabinet is the sum of the capacities of its shelves. The capacity of a shelf currently occupied by chemicals is $\text{currCapacity}(s_{m}^{n})$.

Affinity-adjacent chemicals may be combined into the same container. The cost of a container is orders of magnitude less than the cost of a cabinet; as such, we assume an infinite supply of containers but a finite supply of cabinets.

Let $\text{currVolume}(x)$ denote the current volume chemical $x$ occupies within its container, and let $\text{combine}(y, z)$ be the volume of the combined quantities of chemicals $y$ and $z$, which in either case may be less than the volume of their respective containers. Two instances of the same chemical $v$ and $w$ can be combined by coalescing their respective vertices in $G$. 

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3.4 Chemical Disposal

Let $D = \{d_1, d_2, \ldots, d_k\}$ be the set of containers for chemical disposal. Each container has a maximum volume associated with it, denoted $\maxVolume(d_m)$. The current volume of the container $d_m$ is $\currVolume(d_m)$.

Thus, if $(v, u) \in E$, then $v$ and $u$ cannot be combined in the same container $d_m$ (e.g., $\interact(v, u) = \dagger$), so a new container must be added: $d_{m+1}$. If $(v, u) \notin E \land \vol(v) + \currVolume(d_m) \leq \maxVolume(d_m)$, then $v$ can be combined with $u$ in the container $d_m$. Affinity-adjacent chemicals are assumed to be combined into the same container, assuming the maximum volume of the container allows it.

3.5 Characterization of a Solution to the Chemical Storage Problem

Given a chemical interference graph $G$, ChemStor computes a pair of functions $f : V \rightarrow \{1, 2, \ldots, |C|\}$ and $g : V \rightarrow \mathbb{N}^+$ which assigns each chemical (vertex) to a specific storage location within a cabinet and on a shelf, or (cabinet, shelf). If $(f(v), g(v)) = (m, n)$, then chemical $v$ is assigned to shelf $s^m_n$ in cabinet $c_m$, $1 \leq n \leq |S(c_m)|$.

A legal chemical storage solution must satisfy the Chemical Reactivity Constraint, which states that two interfering chemicals cannot be stored in the same cabinet:

$$f(v) \neq f(u) \ \forall (v, u) \in E \quad (2)$$

A more permissive variant of the Chemical Reactivity Constraint allows two interfering chemicals to be stored in the same cabinet, but on different shelves:

$$p_1 = f(v) \neq f(u)$$

$$p_2 = f(v) = f(u) \land g(v) \neq g(u) \quad (3)$$

$$p_{12} = p_1 \lor p_2 \ \forall (v, u) \in E$$
A legal chemical storage solution must also satisfy the *Storage Capacity Constraint*, which states that the sum of the capacities of the containers assigned to each shelf in each cabinet cannot exceed that shelf’s storage capacity:

\[
\sum_{v \in V | f(v) = m, g(v) = n} \text{currVolume}(v) \leq \maxCapacity(s^n_m) \leq \text{maxCapacity}(s^n_m)
\]

(4)

\[1 \leq m \leq |C|\]

\[1 \leq n \leq |S(c_m)|\]

### 3.6 Satisfiability Modulo Theories

*ChemStor* uses a class of logical formula solvers, Satisfiability Modulo Theories (SMT), to solve a given storage or disposal problem instance. An SMT solver determines whether a problem instance is “decidable”, or can be answered by a simple “true” or “false”. SMT problems support linear inequalities (e.g., \(x + 5y - 2z \leq 5\)), equalities involving uninterpreted terms or functions (e.g., \(f(u, v) = f(g(v), u)\)), Boolean logic (e.g., \(a \land b\)), and in some cases quantifiers (e.g., \(\forall a (a \in \mathbb{N}) (a > 0)\)).

SMT-based problems are expressed as a series of mathematical constraints. These constraints define the valid range of values variables can take for a solution. SMT equations are very expressive and can take one or many of the form(s) noted above. Once these equations are defined, they are used as input to an SMT solver. If the solver can find a solution which satisfies the constraints, it provides a model, or the values of all the variables. If no solution can be found, the solver simply returns “false”.

### 3.7 SMT Constraints

To use a SMT solver to solve a *ChemStor* problem instance, we first convert the Chemical Storage Problem, described in § 3.5, into a set of SMT equations. Each chemical \(v\) must be assigned to exactly one shelf \(s^n_{m_v}\) in exactly one cabinet \(c_{m_v}\). We accomplish this using the
following constraints:

$$m_v \in \mathbb{Z}, 1 \leq m_v \leq |C|$$

(5)

$$n_v \in \mathbb{Z}, 1 \leq n_v \leq |S(c_k)| \land k == m_v$$

(6)

If $v$ is a previously stored chemical, then the values for $m_v$ and $n_v$ are known a priori and are encoded as SMT constants.

The second constraint, the Chemical Reactivity Constraint, guarantees that no pair of chemicals stored in the same cabinet can interact dangerously, and can be expressed as an SMT constraint as follows:

$$\forall u, v \in V | m_u == m_v \text{ interact}(u, v) \neq \dagger.$$  

(7)

The more permissive variant of this constraint, Eq. (3), guarantees that no pair of chemicals stored in the same shelf in the same cabinet can interact dangerously, and can be expressed as an SMT constraint as follows:

$$\forall u, v \in V | m_u == m_v \land n_u == n_v, \text{ interact}(u, v) \neq \dagger.$$  

(8)

Finally, the Storage Capacity Constraint (Eq. (4)) expresses the Storage Capacity Constraint in a form that is already SMT-compatible.

### 3.8 Coalescing Strategy

As defined in §3.2, an affinity edge $(u, v) \in A$ represents two containers that store identical chemicals. Let $t(u)$ denote the chemical “type” of $u$. In ChemStor’s case, the reactivity groups described in §3.1 comprise the different “types” to which chemicals may belong, like
“acid” and “base.” In Eq. (4), \( \text{maxVolume}(v) \) represents the volume of the container that holds chemical \( v \). Let \( \text{currVolume}(v) \leq \text{maxVolume}(v) \) denote the volume of the chemical held in the container. To reduce demands on limited storage space, it may be possible to consolidate multiple instances of the same chemical \( (u \text{ and } v) \) into \( u \)'s container if

\[
\text{currVolume}(u) + \text{currVolume}(v) \leq \text{maxVolume}(u). \tag{9}
\]

Here, the user no longer needs to store \( v \)'s container, and \textit{ChemStor} can eliminate all of \( v \)'s associated SMT constraints.

We implement this feature as a coalescing (vertex merging) operation applied to the chemical interference graph prior to calling the SMT solver; in practice, coalescing opportunities could be incorporated directly into the SMT formulation as well.

Fig. 2 illustrates coalescing. Here \( u \) represents 150 mL of hydrochloric acid in a 300 mL container and \( v \) represents 150 mL of hydrochloric acid in a 300 mL container. Without coalescing, the shelves would use a combined 600 mL of volume to store \( u \) and \( v \). However, with coalescing, \textit{ChemStor} combines them into a single container, reducing the storage requirement to 300 mL.

![Diagram](A)

![Diagram](B)

Figure 2: Demonstrating the coalescing strategy. The affine edge (dotted line) in (A) allows \textit{ChemStor} to combine those chemicals into one vertex as shown in (B), as long as the volumes \( v + v' \leq \text{maxVolume}(v, v') \).
### 3.9 De-Coalescing Strategy

In some cases, it may be necessary to *split* one chemical container into two or more containers; *ChemStor* addresses this behavior through *de-coalescing*. As a motivating example, suppose that a user tries to store 300 mL of hydrochloric acid in a cabinet with three shelves, as shown in Fig. 3. Due to pre-existing chemicals allocated to storage, only 100 mL of space is available on each shelf. In this case, it makes sense to *split* the hydrochloric acid into three 100 mL containers; otherwise, a legal storage solution cannot be found. We implement this strategy using de-coalescing (vertex splitting).

*ChemStor* is allowed to de-coalesce a vertex \( v \) into a given number of \( p \) parts, each having a volume no more than \( \text{vol}(v)/p \). This is expressed using conditional notation within our solver; due to the inherent complexity of this constraint, we describe it conceptually here. If there are \( q \) shelves that do not interact negatively with \( v \) whose combined available capacity is greater than \( \text{vol}(v) \), but whose individual available capacities are smaller than \( \text{vol}(v) \), then we can split \( v \) into an equal number of \( p \) parts, where \( p \) is \( \text{vol}(v) \) divided by the greatest common divisor of the available capacities of the available capacities of the \( q \) shelves. We can then de-coalesce as described above, and the resulting \( p \) instances of chemical \( v \) can be stored on the \( q \) shelves either directly or after further coalescing.

Figure 3: Demonstrating the de-coalescing strategy. To store a chemical whose volume exceeds the capacity of any one shelf (A), *ChemStor* de-coalesces vertices and splits the chemical into \( p \) parts to derive a feasible storage configuration (B).
3.10 No Solutions

There are instances when ChemStor might not converge to a legal solution (in this context, a “legal solution” is one whose constraints have been met, *e.g.*, all chemicals stored in a cabinet have no adverse reaction should they interact). In some cases, this may be in part due to constraints imposed by the set of chemicals pre-assigned to storage locations. One possibility is to unassign all of these vertices and generate a new SMT problem instance. If this second instance is successfully solved, then a legal storage solution has been found, albeit one that may require a significant rearrangement of chemicals stored in the cabinets. If the second instance cannot be solved, then the user is informed that no legal storage solution is possible using the existing resources.

4 Results

We implemented ChemStor using the Python programming language and z3\(^{21}\) as our SMT solver. All experiments were performed on a 64-bit Windows 10 Dell Laptop with an Intel(R) Core(TM) i5-7200U CPU @ 2.50 GHz with 8.00 GB of RAM. The code is available at https://github.com/lilott8/BioScript.

To test the efficacy of ChemStor, we used it to reproduce a number of real-world destructive chemical storage and disposal incidents. In some cases, details regarding the storage resources were sparse or non-existent; in these examples, we made reasonable assumptions about common storage cabinet sizes and quantities, chemical volumes, and chemical taxonomies. For each real-world incident in Table 2, we averaged run times across 100 runs. In each case, ChemStor is able to derive a safe and valid storage or disposal solution in a fraction of a second.

Table 3 reports the ability of ChemStor to handle storage problems which necessitate the use of our coalescing and de-coalescing strategies (i.e., valid solutions are unable to be found without combining or splitting containers of chemicals). ChemStor was able to find a
Table 2: Results from using ChemStor to solve chemical storage and disposal problems from real-life incidents. In these incidents, faulty storage or disposal configurations caused lab fires, explosions, or human harm and incurred significant damages to lab spaces. All run times were averaged across 100 tests. ChemStor was able to find a safe chemical storage or disposal configuration for each incident in a few milliseconds.

<table>
<thead>
<tr>
<th>Incident</th>
<th>Avg. Run Time(ms)</th>
<th>No. of Chemicals</th>
<th>No. of Cabinets</th>
<th>No. of Shelves</th>
<th>Solution Found</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tetrachlorethylene+Nitric Acid[^22]</td>
<td>5.523</td>
<td>2</td>
<td>1</td>
<td>4</td>
<td>Yes</td>
</tr>
<tr>
<td>Hexane Explosion[^9]</td>
<td>2.105</td>
<td>7</td>
<td>1</td>
<td>7</td>
<td>Yes</td>
</tr>
<tr>
<td>Methanol+Nitric Acid[^24]</td>
<td>2.386</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>Yes</td>
</tr>
<tr>
<td>Benzene+Urea+Benzotrichloride[^22]</td>
<td>4.450</td>
<td>3</td>
<td>1</td>
<td>3</td>
<td>Yes</td>
</tr>
<tr>
<td>Lithium Aluminium Hydride Fire[^7]</td>
<td>7.043</td>
<td>3</td>
<td>1</td>
<td>3</td>
<td>Yes</td>
</tr>
<tr>
<td>H₂O₂+Sulfuric Acid + Acetone[^22]</td>
<td>10.086</td>
<td>3</td>
<td>1</td>
<td>4</td>
<td>Yes</td>
</tr>
<tr>
<td>Formaldehyde+Benzene[^22]</td>
<td>11.338</td>
<td>3</td>
<td>1</td>
<td>4</td>
<td>Yes</td>
</tr>
<tr>
<td>Univ. of Tennessee, Knoxville Fire[^4]</td>
<td>23.177</td>
<td>4</td>
<td>1</td>
<td>4</td>
<td>Yes</td>
</tr>
<tr>
<td>Broken Beaker of Barium Oxide[^5]</td>
<td>1.272</td>
<td>11</td>
<td>3</td>
<td>3</td>
<td>Yes</td>
</tr>
<tr>
<td>Lab Fire at Ohio State University[^1]</td>
<td>1.241</td>
<td>9</td>
<td>2</td>
<td>3</td>
<td>Yes</td>
</tr>
</tbody>
</table>

safe storage configuration for all the synthetic storage problems where one exists, denoted by “Yes” in the Valid Solution Found column. In the case of the two synthetic failures, ChemStor was unable to find a safe storage configuration, as was expected. The two failing test cases demonstrate problem instances where a valid solution is impossible and the likelihood of an unsafe incident is significant. In these two cases, the coalescing and de-coalescing strategies would not prove helpful as the volume constraint on a shelf prevents a chemical from being safely stored. As in Table 2, we average run times over 100 runs, and note that every test returns in a few milliseconds.

5 Conclusions

ChemStor generates safe storage and disposal configurations that are provably safe, given the chemicals have assigned EPA/NOAA reactivity groups. In all of our test cases, ranging from real-world to synthetic, ChemStor converged in less than one second, which indicates that realistic storage/disposal problem instances yield SMT problem instances that can be
Table 3: Synthetic tests demonstrating the efficacy of ChemStor’s coalescing and decoalescing strategies. All run times were averaged across 100 tests. We crafted tests for the edges case: restrictive placement, relaxed placement, coalescing success or failure, and decoalescing success or failure. If a solution could not be found, the corresponding column is marked with a “No”.

<table>
<thead>
<tr>
<th>Test</th>
<th>Avg Run Time (ms)</th>
<th>No. of Chemicals</th>
<th>No. of Cabinets</th>
<th>No. of Shelves</th>
<th>Solution Exists</th>
<th>Solution Found</th>
</tr>
</thead>
<tbody>
<tr>
<td>Full Cabinet</td>
<td>0.64</td>
<td>5</td>
<td>1</td>
<td>4</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Compatible Chemicals</td>
<td>39.54</td>
<td>5</td>
<td>3</td>
<td>4</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Combine Two Tests</td>
<td>142.96</td>
<td>8</td>
<td>4</td>
<td>4</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Pass Coalescing</td>
<td>4.94</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Pass Decoalescing</td>
<td>10.60</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Fail Coalescing</td>
<td>3.14</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>Fail Decoalesce</td>
<td>4.77</td>
<td>1</td>
<td>1</td>
<td>2</td>
<td>No</td>
<td>No</td>
</tr>
</tbody>
</table>

solved rapidly. This is important, as it enables ChemStor to provide real-time advice to users before dangerous storage and disposal mistakes are made.

In its current form, ChemStor has some significant limitations. For example, as noted earlier, ChemStor’s problem instance is difficult to solve; and because of the difficulty of the graph coloring problem, parallelization is of little help. While ChemStor is capable of accepting a problem instance containing millions of chemicals, problems of that magnitude might not converge on a solution quickly. Additionally, ChemStor doesn’t account for chemical properties like concentrations or temperatures; obviously these properties heavily influence the reactivity of the chemicals. Also, the notion of a “cabinet” in ChemStor is abstract, and differentiating between, say, a refrigerator and a room-temperature shelf is an important distinction when storing a chemical with a flash point near room temperature. Finally, the ChemStor “container” is an abstract volume and does not capture the real-world container dimensions that dictate shelf or cabinet capacity. Future versions of ChemStor should address these shortcomings, and since ChemStor is an open-source project, we welcome others to add additional capabilities to the software and use it in their own projects.

In the near future, ChemStor can be incorporated into the various technological assistants that are gaining popularity in workplaces and homes. For example, by including ChemStor
in an electronic laboratory notebook, the notebook software could automatically suggest chemical disposal strategies after each experiment. Cameras in augmented reality systems could actively scan the workplace and use *ChemStor* to identify unsafe chemical storage situations before accidents occur, and microphones could listen for employees’ questions about storage and disposal. These scenarios are not that far-fetched—software developers are already working on voice-based assistants for chemists, and integrating *ChemStor* into these tools seems relatively straightforward. Finally, including *ChemStor*’s recommendations in home voice assistants like Apple’s Siri and Amazon’s Alexa could significantly reduce the number of chemical-related injuries and accidents that occur in homes.

**Acknowledgement**

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**References**


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